# THE $T_g$ DISPLACEMENT MEASUREMENTS: A WAY TO FORESEE THE PHYSICAL BEHAVIOUR AND THE USE OF GLASSY POLYMERS

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The effect of ageing temperature (below  $T_g$ ) on physical ageing of glassy PET has been investigated by differential scanning calorimetry. The position of the glass transition endotherm was found to be strongly dependent on the annealing conditions (time, annealing temperature). A single relaxation time model is proposed for the analysis of physical ageing.

The variations of the equilibrium relaxation time  $\tau_{iso}$  with annealing temperature allow the determination of the parameters of the model. Finally, using these constants, one can determine the thermal past and foresee the thermal future of unknown samples which are of prime importance in processes using temperatures around the glass transition temperature.

Keywords: Tg displacement, glassy polymers

#### Introduction

It is of prime importance to foresee the physical behaviour (i.e. evaluate the ageing) in the use of a material, particularly for glassy polymeric materials. It holds in standard use for wear and tear of things as well as in industrial processes where the material (or a preform of the final product) is heating (for softening) above its glass transition temperature  $(T_g)$  before the final forming process. Indeed, because of the lack of thermodynamic equilibrium in such glassy materials, relaxation processes occur during ageing at temperatures lower than  $T_g$ .

It is well known that the value of the glass transition temperature depends on many parameters such as the following:

i) the nature of the polymer;

ii) the thermal history (this includes preparation as well as ageing);

iii) the different stresses and constraints (mechanical, illuminatiton,...). However, in spite of the great number of parameters which influence the value of  $T_g$ ,

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it is possible to use a judicious selection of experiments to approach ageing phenomena in glassy polymers by means of measurements of  $T_g$ . As number of changes in physical properties (optical, mechanical, thermal,...) are observed when the material is heating (or cooling) through the glass transition region, different methods could be used but the majority of them is connected with thermal analysis methods. Moreover all transitions which imply thermal exchanges will be more or less observable by DSC means and can be characterized by their energies and their temperatures.

The aim of this paper is to develop a method which, from DSC measurements, allows for glassy polymers an estimation of the thermal past and/or a prediction of the future. Experimental results presented here were carried out on polyethylene terephthalate (PET) glassy samples.

## **Sample preparation**

The samples have been prepared by quenching ( $\approx 10^2 \text{ deg} \cdot \text{s}^{-1}$ ) from the melt of a granule of PET directly into the sample pans of the calorimeter (Perkin Elmer, system 4). In order to obtain a good reproducibility in ageing studies, the same sample was used for a series of experiments. This is possible by cooling the sample, after heating it through the transition region, back to the ageing temperature. This thermal cycle (D $\rightarrow E \rightarrow F \rightarrow B \rightarrow C$  in Fig. 1), called rejuvenation, leads to the restoration of the as-prepared state (no degradation was observed by thermogravimetry as well as X-ray diffraction). The glassy nature of the samples



Fig. 1 Change of enthalpy during cooling  $(A \rightarrow B \rightarrow C)$ , ageing  $(C \rightarrow D)$  and reheating  $(D \rightarrow E \rightarrow F)$ .  $\Delta T_g$  indicates the range of variations of  $T_g$ 

was probed by X-ray diffraction. Finally the value of the glass transition temperature is measured directly on the curve as shown in Fig. 2.



Fig. 2 Determination of T<sub>g</sub> on a DSC curve for various heating rates: a) r=15 deg.min<sup>-1</sup>; b)
r=20 deg.min<sup>-1</sup>; c) r=25 deg.min<sup>-1</sup>; d) r=30 deg.min<sup>-1</sup>; e) r=40 deg.min<sup>-1</sup>; f) r=50 deg.min<sup>-1</sup>;
g) r=60 deg.min<sup>-1</sup>. T<sub>g</sub> is obtained from the intercept of the slope on the left-hand part of the peak with the base line

## Methods and models

The main parameter which characterizes an ageing process is the relaxation (or retardation) time  $\tau$  which occurs in the relaxation equation:

$$\frac{\partial H}{\partial t} = -\frac{H - H_{\rm e}}{\tau} + C_{\rm pg} r \tag{1}$$

where H is the current enthalpy,  $H_e$  the equilibrium enthalpy (when the ageing is achieved), t the time, r the heating rate and  $C_{pg}$  the heat capacity in the glassy state. Other authors use several time constants or distribution of time constants [1–3], but it has been shown [4] that, if the range of annealing temperatures used during the relaxation process studies is close to  $T_g$ , a single relaxation time is a good approximation.

We consider, hereafter, a simple model using a single relaxation time which separates the temperature dependence F(T) and the structural variation G(S) (cooperative effects). In this model, used in many previous works [4-6] the relaxation time could be given by [7-9]:

$$\ln \tau = \ln a - b.T - c. (H - H_e) \tag{2}$$

where the constants a, b, c depend on the material. Moreover, in a first approach, we may suppose that the difference  $\Delta C_p$  between the specific heats in the liquid and in the glassy states is independent of the annealing temperature  $(T_a)$ , annealing duration and heating rate; then a linear relationship exists between the variation of enthalpy and the variation of temperature:

$$H - H_{e} = \Delta C_{p} \cdot (T_{f} - T)$$
(3)

 $T_{\rm f}$  is the 'fictive' temperature (for which the curve H(T) followed during heating reaches the extrapolated equilibrium curve  $H_{\rm e}(T)$ ).

Using ageing time, annealing temperature and heating rate as parameters, the proposed method which leads to the different constants of the material, requires two kinds of experiments:

#### Dependence of $T_g$ on heating rate

During heating or cooling, at different rates r, of samples of the same age, we could assimilate the continuous change of temperature to a series of instantaneous small variations  $\Delta T$  followed by an isothermal hold of duration  $\Delta t = \Delta T/r$ . The structure will readily relax to its equilibrium state if the relaxation time is smaller then  $\Delta t$ ; when  $\tau$  is larger than  $\Delta t$  the structure will remain in the glassy state. So we may define the glass transition temperature  $T_g$  as the temperature where the relaxation time  $\tau$  becomes comparable with the isothermal hold  $\Delta t$  and consequently  $r \cdot \tau(T_g)$  is constant. Thus

$$\ln r = -\ln a + b T_g + c (H - H_e) + \text{constant}$$
(4)

and (with Eq. (3))

$$\ln r = b \cdot T_{g} - c \cdot \Delta C_{p} \cdot T_{g} + c \cdot \Delta C_{p} \cdot T_{f} + \text{constant}$$
(5)

The last term depends on ageing duration, but for the same ageing  $T_{\rm f}$  is constant. So

$$\frac{\mathrm{d}\ln r}{\mathrm{d}T_{\mathrm{g}}} = b - c \cdot \Delta C_{\mathrm{p}} \tag{6}$$

Figure 3 shows the good agreement between this model and the experimental results. When the measurements are carried out with cooling from the liquid state, this method leads to d ln  $r/dT_g=b$  (because, in this case, the departure from the liquid equilibrium vanishes for temperatures greater than  $T_g$ ).



Fig. 3 Change of  $T_g$  against logarithm of heating rate

# Dependence of $T_g$ on heating

In this case, the heating rate and the annealing temperature are kept constant. As in the above section, the variations of H and of  $T_g$  are linked by the linear relationship

$$H_{2}-H_{1}=(b-c\cdot\Delta C_{p})\cdot(T_{g1}-T_{g2})/c$$
(7)



Fig. 4 Displacements of  $T_g$  with ageing time for various annealing temperatures (r=20 deg·min<sup>-1</sup>): a)  $T_a=50^{\circ}$ C; b)  $T_a=55^{\circ}$ C; c)  $T_a=60^{\circ}$ C; d)  $T_a=65^{\circ}$ C; e)  $T_a=70^{\circ}$ C

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For two ageing duration  $t_1$  and  $t_2$  ( $H_1$ ,  $H_2$ ,  $T_{g1}$ ,  $T_{g2}$  respectively), the glass transition is reached when the relaxation times are equal. Then the variations of  $T_g$ (Fig. 4) with time can be described by

$$\frac{\mathrm{d}\,\Delta T_{\mathrm{g}}}{\mathrm{d}t} = -\frac{\Delta T_{\mathrm{g}} \exp\left(\left[b - c \cdot \Delta C_{\mathrm{p}}\right] \cdot \Delta T_{\mathrm{g}}\right)}{\tau_{\mathrm{iso}}} \tag{8}$$

with  $\tau_{iso}=a \cdot \exp\{-b \cdot T_g\}$  and  $\Delta T_g=T_{ge}-T_g$  ( $T_g$  and  $T_{ge}$  are respectively the glass transition temperatures after an ageing duration t and after complete ageing). The curves in Fig. 4 obtained by fitting the experimental results and the Eq. (7) lead to the isothermal relaxation time  $\tau_{iso}$ . The changes of  $\ln \tau_{iso}$  with annealing temperature enable the determination of  $a=8\cdot10^{41}$  h and b=0.27 K<sup>-1</sup> (Fig. 5). Other material constants c=0.11 gJ<sup>-1</sup> and  $\Delta C_p=0.54$  Jg<sup>-1</sup>K<sup>-1</sup> are obtained from the heating rate dependence measurements and by calorimetric means.



Fig. 5 Change of the equilibrium relaxation time  $\tau_{iso}$  against annealing temperature

Figure 6 shows the variations of the initial glass transition temperature  $T_{gi}$  (fresh sample) and of the equilibrium value  $T_{ge}$  with the annealing temperature. The initial  $T_{gi}$  increases with the temperature  $T_a$  while the equilibrium value  $T_{ge}$  decreases. It is clear that these variations lead to a limit for  $T_a$  (when  $T_a \approx T_{ge} \approx T_{gi}$ ); indeed the higher is  $T_a$ , the lower is the equilibrium value. For the lowest ageing temperatures, the relaxation phenomena are so long that measurements are not possible compared with the experimental time and for the highest



Fig. 6 Variations of the initial and of the equilibrium glass transition temperatures with annealing temperature. Curves are extrapolated behaviours

 $T_{\rm a}$  the material relaxes so fast that the measurements cannot be considered to be significative.

## Applications

Let us consider a batch of glassy PET preform of unknown ageing and stocked at temperatures between 15° and 20°C. Because of the structural relaxation during this ageing time, the final forming process (which generally implies heating above  $T_g$ ) will be different (due to the  $T_g$  changes). So it is quite important to be able to estimate the thermal past and the future of these preforms. Figure 6 shows the variations of  $T_{gi}$  and of  $T_{ge}$  for the ageing temperature range considered. Using these values and the relaxation constants of PET, we could draw the Time-Temperature ageing diagram of this batch (Fig. 7). In this diagram, the glass transition temperature of a preform must fall in the shaded are which represents the ageing zone.

Now, it is sufficient to make a statistical study of the glass transition temperature of this batch. Results reported in Fig. 8 do not show significative differences between the three regions of preforms studied (with respect to the different cooling conditions in the matrix after injection, we have arbitrarily distinghished three regions of analysis: the external sides and the middle). Then the mean value of  $T_g$  (74°C) reported in Fig. 7 indicates a stockage duration of 1000 h. In the same way, for these ageing conditions, Fig. 7 does not show no-



FIg. 7 Time- $T_g$  diagram: the shaded area indicates the ageing zone of the material for the considered stockage temperature range (15°-20°C)



Fig. 8 Distribution function of the  $T_g$  measured of a batch of unknown PET preforms (S1, S2 and M indicates the sides and the middle of the analyzed samples, respectively)

ticeable changes of the glass transition temperature before 5000 hours ( $\approx 6$  months) of ageing. Then, for the youngest preforms, the forming process could be the same whereas for the oldest ones the temperature of the processes must be increased up to twenty degrees.

#### References

- 1 A. J. Kovacs, J. Polymer Sci., 30 (1958) 131.
- 2 A. J. Kovacs, Fortschr. Hochpolym.Forsch., 3 (1963) 394.

- 3 N. Clavaguera, M. T. Clavaguera-Mora, S. Surinach, M. D. Baro, J. Non-Crystalline Solids, 104 (1988) 283.
- 4 J. P. Larmagnac, J. Grenet and P. Michon J. Non-Crystalline Solids, 45 (1981) 157.
- 5 J. M. Saiter, A. Assou, J. Grenet and C. Vautier, Phil. Mag. B, 64 (1991) 33.
- 7 C. T. Moynihan, A. J. Easteal, J. Wilder and J. Tucker, J. Phys. Chem., 78 (1974) 2673.
- 8 A. J. Kovacs, J. M. Hutchinson and J. J. Alkonis, Structure of Non-Crystalline Materials, edited by P.H. Gaskel, Taylor & Francis, London 1977, p. 153.
- 9 A. Q. Tool, J. Am. Ceram. Soc., 29 (1946) 240.

**Zusammenfassung** — Mittels DSC wurde der Einfluß der Alterungstemperatur (unterhalb  $T_g$ ) auf das physikalische Altern von glasartigen PET untersucht. Die Lage der Glasumwandlungsendothermen hängt stark von den Temperungsbedingungen (Dauer, Temperungstemperatur) ab. Es wird ein Relaxationszeitmodell für die Analyse physikalischen Alterns vorgeschlagen.

Die Parameter dieses Modelles können aus der Änderung der Gleichgewichtsrelaxationszeit  $\tau_{iso}$ mit der Temperungstemperatur ermittelt werden. Unter Benutzung dieser Konstanten kann die thermische Vergangenheit unbekannter Proben bestimmt und die thermische Zukunft derselben vorhergesagt werden, was für Vorgänge bei Temperaturen um den Glasumwandlungspunkt von primärer Wichtigkeit ist.